

Association Testing in Related Individuals

Family data is correlated that could lead to inflation in test statistics if not accounted for. Many genetic studies contain related individuals. Family-based studies were developed to avoid bias due to population structure; Biological family members are genetically matched.

Most behavioral and environmental factors do not alter DNA, so SNP associations are unlikely to be confounded EXCEPT confounding by ancestry.



Population Stratification Bias

- For case control studies, population structure means bad matching; cases and controls come from different genetic populations.
- For cohort/cross-sectional studies with quantitative phenotypes, if the phenotype and genotype distributions both differ by population then population stratification bias can occur.
- If a population consists of a mixture of subpopulations and it is not accounted for in the analysis, false evidence for association may result.
- Spurious association only occurs when there is a difference in BOTH genotype and phenotype distribution with subpopulations.

Designs for Family-Based Studies

- Early-onset phenotypes:
 - Case-parent trios (where child is effected) - Transmission disequilibrium test (TDT)
- Late-onset phenotypes:
 - Discordant siblings - sub-TDT/conditional logistic regression
- General designs
 - Nuclear or extended families - Family-based association test (FBAT)

We'll mostly focus on case-parent trios and TDT tests.

Case-Parent Trios

In this design we collect samples of trios; Two parents and one affected child (affection status of parents are not considered). The idea is under Mendel's laws, heterozygous parents transmit each allele with equal probability (1/2) regardless of population structure. If there is preferential transmission of a specific allele from parents to affected offspring it indicates that allele is associated with the disease.

Transmission Disequilibrium Test (TDT)

Tests whether a particular marker allele is transmitted to affected offspring more frequently than expected. Non-transmitted alleles act as matched controls.

H_0 : No association or no linkage

H_a : Variant is associated with disease/trait (and is not due to population structure)

Notation:

Not transmitted	Transmitted	
	A	B
	A	B
	a	b
B	c	d

- a = number of AA parents
- b + c = number of AB parents
 - b = Number of AB parents transmitting B to affected child
 - c = Number of AB parents transmitting A to affected child
- d = number of BB parents

Under the null we would expect:

$$P(AB \rightarrow A) = P(AB \rightarrow B) = \frac{1}{2}$$

$$b \approx c \text{ and } \frac{b}{b+c} \approx \frac{1}{2}$$

The test statistic follows a McNemar test:

$$\text{TDT} = (b - c)^2 / (b + c), \sim \chi^2 \text{ with } df = 1$$

We observe this is only a function of the heterozygous parents, homozygous parents provide no information.

Discordant Siblings

- TDT unit of analysis is affected child + parents.

- Discordant siblings - unit of analysis is sibships with at least one affected and one unaffected sibling
- Analysis possibilities:
 - Cochran-Maentel-Haenszel test
 - Conditional Logistic Regression
- Like TDT these tests are conditioning on the genotypes in the family
 - TDT: conditioning on the parent's alleles
 - Sibs: conditioning on the observed genotypes in the sibship

General Family Structures

- Family Based Association Test (FBAT) and other similar tests (requires specialized software)
- Determine the expected genotypes of the affected individuals conditional on the family structure
- Use this to create a score test comparing observed and expected genotypes
- Same idea as parent-offspring trios or case-control sibships: conditioning on the observed genotypes

Unconditional Tests

- TDT, sTDT, FBAT and other family based association tests are conditional tests
- These tests are immune to population structure bias but often ignore information that can be used to assess association when population structure is not a concern
 - Homozygous parents
 - Sibships where the case and control have the same genotype
- Modern analyses can account for population structure using ancestry information available with genome-wide data
- Unconditional analyses account for the family correlation and make use of all the observed data
- These analyses tend to be more powerful than the conditional family-based tests

Review: For unrelated (independent) subjects we can use standard linear or logistic regression. Including related individuals in the analysis violates the assumption of independence, causing inflation in the test statistics.

$$Y_i = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i3} + \dots + e_i,$$

where $i = 1, \dots, n$, and $e_i \sim N(0, \sigma_e^2)$

i.e., $\text{var}(Y_i) = \sigma_e^2$, $\text{cov}(Y_i, Y_j) = 0$ for $i \neq j$

Where X_{i1} is the genotype of the i^{th} person and β_1 is the fixed effect of the SNP. X_{i2} and X_{i3} are covariates.

For related data there are specific methods we can use:

- For quantitative traits use Linear mixed effects models are frequently used for corrected observations for an individual or related individuals.
- Pedigree-specific methods use a variance component that is dependent on the kinship matrix for individuals.

$$Y_i = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i3} + \dots + \mathbf{G} + e_i,$$

where $i = 1, \dots, n$, $e_i \sim N(0, \sigma_e^2)$ and $\mathbf{G} \sim N(0, \phi \sigma_G^2)$, so:

$$\begin{aligned} \text{var}(Y_i) &= \sigma_G^2 + \sigma_e^2 \\ \text{cov}(Y_i, Y_j) &= \phi_{ij} \sigma_G^2 \end{aligned}$$

β : fixed effects, \mathbf{G} : random effect, e_i : individual error

ϕ_{ij} : coefficient of relationship (twice the kinship coefficient) between individuals i and j (=0 if unrelated, 1 for twins and for an individual with themselves)

We can see the mixed effects model adds a G variable to account for genetic variance component.

For association analysis of quantitative traits, if X_1 is the SNP then the test $H_0: \beta_1 = 0$ is a test of association just as for the linear model for unrelated subjects. The regression estimate beta is exactly the same as in simple linear regression.

In either case G is not tested for significance. If we want to test for heritability we estimate variance of G.

Common software: GCTA, SOLAR, R GMMAT package, Genesis R/Bioconductor package.

Dichotomous Traits

- Logistic mixed effects can be used to account for relationships
 - Fit using penalized quasi-likelihood method
 - Requires iterative matrix inversion - can be very slow
- Alternative: Logistic model with Generalized Estimating Equations (GEE)
 - Accounts for correlated observations in a general way
 - Produces a "robust" variance estimate to account for correlation
 - Tends to result in inflated Type-I error
 - Low frequency SNPs primary problem
 - Extent of inflation varies

In this course we focus on quantitative traits to keep things simple.